

# Introduction to Programming: Lecture 5

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# Mark Lists

- ▶ `marks` – as before.
- ▶ Rearrange it so that you have a list of lists in which each list gives the marks obtained by one student.

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= [[10,9], [10,2], [8,10]]
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```
transpose []:xs = []  
transpose xs = (map head xs):transpose (map tail xs)
```

# List notation: ranges

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▶ Arithmetic progressions

$[1, 3..8] = [1, 3, 5, 7]$

$[2, 5..19] = [2, 5, 8, 11, 14, 17]$

▶ Lists in descending order

$[8, 7..5] = [8, 7, 6, 5]$

$[12, 8..-9] = [12, 8, 4, 0, -4, -8]$

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 ("Shahrukh", 29)]
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- ▶ `([Int], Int)` is the type whose members are pairs, the first is a list of integers and the second is an integer.

`([], 67) :: ([Int], Int)`

`([1, 2], 73) :: ([Int], Int)`

## Tuples: `fst` and `snd`

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- ▶ `fst([1,2,3], 'a') = [1,2,3]`
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- ▶ `sumpairlist l = sum ((map sumpairs) l)`

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- ▶ A tuple of type `(String,Int)` can store a student's mark and a marklist is of type `[(String,Int)]`.

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lookUp :: String -> [(String,Int)] -> Int  
lookUp s ((name,marks):l)  
  | (s == name) = marks  
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lookup :: String -> [(String,Int)] -> Int  
lookup s ((name,marks):l)  
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```
getStudMarks :: String -> [[(String,Int)]] -> [Int]  
getStudMarks s = map (lookUp s)
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## Giving Names to complex types

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- ▶ We may then write

```
lookUp :: String -> Marklist -> Int
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getStudMarks :: String -> [Marklist] -> [Int]
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and so on.

# Type definitions

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# The function `zip`

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`[('a',1),('b',2),('c',3)]`
  - ▶ `zip ['a'..'z'] [1..10] ~>`  
`[('a',1),('b',2),...,('j',10)]`

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```
totalMarks (x:xs) =  
  zip (map fst x) (addMarks (map (map snd) (x:xs)))
```

# Idiomatic programming

- ▶ Programming languages are ... **languages!**
- ▶ Like “natural languages”, we can say the same thing in many ways
- ▶ Initially, we use a language in its simplest and most direct form
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- ▶ Initially, we use a language in its simplest and most direct form
- ▶ As we master the language, we learn to use it idiomatically and more effectively
- ▶ To learn a language, you must practice speaking it.

## Example: initial segments

- ▶ Write a Haskell function `initsegs` which returns the list of initial segments of a list.

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initsegs [1,2,3] = [], [1], [1,2], [1,2,3]
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initsegs (x:xs) = [] : map (x:) (initsegs xs)
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## Example: interleave

- ▶ `interleave x l` inserts `x` into all possible positions in the list `l`

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interleave 3 [] = [[3]]
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interleave 3 [2,3] = [[3,2,3], [2,3,3], [2,3,3]]
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interleave 'a' "abcd" =
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["aabcd", "aabcd", "abacd", "abcad", "abcda"]
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interleave x [] = [[x]]
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```
interleave x (y:ys) = (x:y:ys) :
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    map (y:) (interleave x ys)
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## Example: Permutations

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**Exercise:** What is the type of `concatMap`

## Example: Partitions

- ▶ Given a list  $l$  is a collection of nonempty lists  $l_1, l_2, \dots, l_k$  such that  $l = l_1 ++ l_2 ++ \dots ++ l_k$

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- ▶ The type of `part` is `part :: [a] -> [[[a]]]`

```
part [x] = [ [ [x] ] ]
```

```
part (x:xs) = map ([x]:) (part xs) ++  
              map (f x) (part xs)
```

where

```
f x (y:ys) = (x:y):ys
```